

§10-1 Curves Defined by Parametric Equation

*Parameter Equation : $x = f(t), y = g(t)$.

Parameter Curve : $\{(x, y) : x = f(t), y = g(t)\}$.

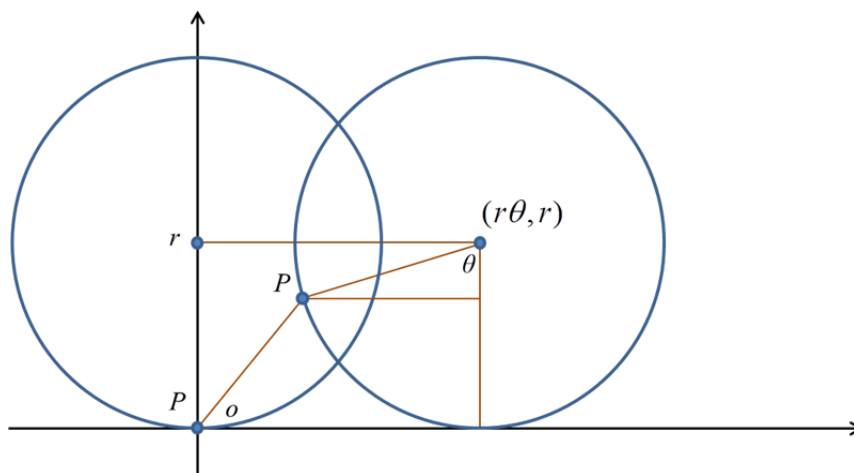
Example 1 : Verify the curve $x = \cos t, y = \sin t, 0 \leq t \leq 2\pi$.

Solution :

The circle : $x^2 + y^2 = 1$

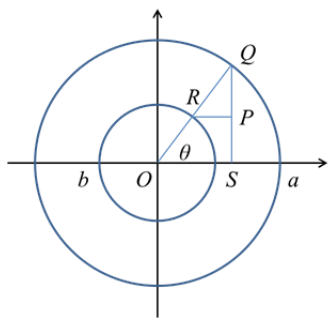
Example 2 : The curve traced out by a point P on the circumference of a circle as the circle rolls along a straight line is called a cycloid. Find parametric equation for the cycloid.

Solution :



$$\begin{aligned} p(x, y) \\ x &= r\theta - r \sin \theta \\ y &= r - r \cos \theta. \end{aligned}$$

Example 3 : Find $P(x,y)$ in terms of Q . What is its parametric curve?



Solution :

$$x = \overline{SO} = a \cos \theta, y = \overline{QS} - \overline{SP} = a \sin \theta - b \sin \theta$$

$$\Rightarrow \cos \theta = \frac{x}{a} \text{ and } \sin \theta = \frac{y}{(a-b)}$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{(a-b)^2} = 1.$$